# ACHARYA NAGARJUNA UNIVERSITY : CENTRE FOR DISTANCE EDUCATION M.Sc. – Statistics - Program code: 138

# **Program Structure**

Program code	Program	Internal assessment	External exams	Max. Marks	credits
SEMISTER					
101ST24	Probability Theory and Distributions	30	70	100	4
102ST24	Statistical Computing Using R	30	70	100	4
103ST24	Estimation	30	70	100	4
104ST24	Sampling Theory	30	70	100	4
105ST24	PRACTICAL-I Statistical Software using R (Papers on 101ST24 and 102ST24)			100	4
106ST24	PRACTICAL-II (Papers on 103ST24 and 104ST24)			100	4
SEMISTE	R 2				
201ST24	Multivariate Analysis	30	70	100	4
202ST24	Testing of Hypothesis	30	70	100	4
203ST24	Theory of Linear Estimation and Analysis of Variance	30	70	100	4
204ST24	Linear Models and Applied Regression Analysis	30	70	100	4
205ST24	PRACTICAL-I Statistical Software using SPSS and R (Papers on 201ST24 and 202ST24)			100	4
206ST24	PRACTICAL-II (Papers on 203ST24 and 204ST24)			100	4
SEMISTE	R 3				
301ST24	Design of Experiments	30	70	100	4
302ST24	Statistical Quality Control	30	70	100	4
303ST24	Actuarial Statistics	30	70	100	4
304ST24	Reliability-I	30	70	100	4
305ST24	Practical-I Statistical Software using SPSS and R (Papers on 301ST24 and 302ST24)			100	4
306ST24	Practical-II (Papers on 303ST24 and 304ST24)			100	4
SEMISTE					
401ST24	Econometrics	30	70	100	4
402ST24	Acceptance Sampling Plans	30	70	100	4
402ST24 403ST24	Operations Research	30	70	100	4
403ST24 404ST24	Reliability-II	30	70	100	4
404ST24 405ST24	Practical-I Statistical Software using SPSS and R (Papers on 401ST24 and 402ST24)			100	4
406ST24	Practical-II (Papers on 403 ST24 and 404 ST24)			100	4

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# **SEMESTER-I**

# 101ST24: Probability Theory and Distributions

# Unit I:

Classes of sets, fields,  $\sigma$  fields, minimal  $\sigma$  fields, sequence of sets, limit supremum and limit infimum of sequence of sets, measure, probability measure, properties of measure, axiomatic definition of probability, continuity theorem of probability, conditional probability, statistical independence of events, probability on finite sample spaces, geometrical probability.

#### Unit-II

Measurable functions, notation of random variable, distribution function, properties of distribution, vector of random variables, statistical independence, concepts of joint, marginal and conditional distributions, mathematical expectation, conditional expectation, characteristic function, its properties. Inversion formula, characteristic functions and moments. Moments inequalities-Markov, Schwartz, Jensen, Holder, Minkowski, Kolmogrove's, Hajek-Renyi.

#### Unit -III

Convergence of sequence of random variables-Type of convergence-in probability, almost sure, in mean square, in law- their interrelations. Law of large numbers-weak laws: Chebychevs's form of W.L.L.N., Necessary and Sufficient Condition of W.L.L.N. Kintchines form of W.L.L.N., Kolmogrove's S.L.LN for i.i.d. random variables.

### **Unit-IV**

Discrete distributions - Compound Binomial, Compound Poisson, multinomial, truncated Binomial, truncated Poisson distributions and their properties. Continuous distributions-Laplace, Weibull, Logistic and Pareto distributions and their properties.

# **UNIT-V**

Order statistics- distribution function, probability density function (p.d.f.) of single order statistic, joint p.d.f. of order statistics. Distribution of range with applications in rectangular and exponential cases.

# **BOOKS FOR STUDY:**

- 1) Modern probability theory by B.R. Bhat, Wiley Eastern Limited.
- 2) An introduction to probability theory and mathematical statistics by V.K.Rohatgi, John Wiley.
- 3) An Outline of statistics theory-1, by A.M.GOON, M.K. Gupta and B. Dasgupta, the World Press Private Limited, Calcutta.
- 4) The Theory of Probability by B.V. Gnedenko, MIR Publishers, Moscow.
- 5) Discrete distributions N.L. Johnson and S. Kotz, John wiley & Sons.
- 6) Continuous Univariate distributions, vol.1&2- N.L.Johnson and S.Kotz, John Wiley & Sons.
- 7) Mathematical Statistics Parimal Mukopadhyay, New Central Book Agency (P) Ltd., Calcutta.

# **BOOKS FOR REFERENCES:**

- 1) Billingsley, P. (1986): Probability and Measure. Wiley.
- 2) Kingman, J F C and Taylor, S. J. (1966): Introduction to Measure and Probability. Cambridge University Press.
- 3) David, H.A (1981): Order Statistics, 2<sup>nd</sup> Ed, John Wiley.
- 4) David H. A. and Nagaraja H.N.(2003): Order Statistics, 3/e, John Wiley & Sons.
- 5) Feller, W (1966): Introduction to probability theory and its applications, Vol.II, Wiley.
- 6) Cramer H (1946): Mathematical Methods of Statistics, Princeton

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#### **SEMESTER-I**

# 102ST24: Statistical Computing Using R

# UNIT - I:

Introduction to R language: Objects (Atomics) -Basic types, modes and attributes, comments, constants. R-Data Types: character, numeric, integer, logical, complex and raw data types. R-Operators: arithmetic, relational, logical, assignment and miscellaneous operators. R-Variables: variable assignment, data type, finding variables using ls()function, deleting Variables using rm() function, R-I/O console functions-scan(), print(), cat(), format(), setwd() and getwd() functions. R-vectors: creating vectors, vector assignment, manipulating vectors, arithmetic, generating regular sequences, logical vectors, and character vectors, index vectors, selecting and modifying subsets of a vector. Manipulating character vectors using strsplit(), paste(), grep(), gsub() functions; R-factors: creating factor variables, handling factor data, generating factor levels using gl() function.

#### UNIT - II:

R-Matrices: Creating matrices, arithmetic operators on matrices, matrix facilities, forming partitioned matrices, cbind() and rbind() functions, R-Lists: creating a list, naming, accessing and manipulating list elements, converting a list to a vector. R-Data frames: creation, adding rows and variables to data frame, attach() and detach(), working with data frames, data reshaping. Reading and getting data into R using files: reading data and writing data from / to files of type CSV, EXCEL, text and other data type files using the save(), load(), read.csv()and read.table(),write.csv() and write.table() functions. Retrieving files using file.choose(), function.

# UNIT - III:

R – Control Structures: Decision making-if, if-else, ladder if-else, nested if-else, and switch statements. Loops-repeat, while and for statements. Loop control statements -- break and next. R – Functions: function definition, function components, built-in functions, user- defined function, syntax of a function, function arguments, arguments matching, scope and evaluation, calling a function, one-line functions, using default values in functions. Built in R-functions and writing own R-functions or R-codes for small standard statistical problems like finding summary statistics, correlation, one-sample t-test, two-sample t-test and paired samples t-test, etc. Group manipulation using apply family of functions - apply, sapply, lapply and tapply.

# UNIT-IV:

R-Probability Distributions: Computing values of pdf, cdf, quantile and generating samples for bionomial, poission, normal, exponential, Weibull and other prominent distributions using Built in R – functions. Plotting density and cumulative density curves for the distributions. Built in R-syntaxes for the Shapiro-Wilk test of normality, Kolmogorov-Smirnov test for one-sample and two-sample cases, Wilcoxon Mann-Whitney one-sample and two-sample U- tests, chi-square tests for association and goodness of fit. Writing own R-functions or R- codes: Fitting of binomial, Poisson, normal, exponential, Weibull and logistic distributions based on a given frequency data and test for goodness of fit. Solving a non-linear equation using Newton-Raphson method.

# UNIT-V:

R-Graphics: Use of high-level plotting functions for creating histograms, scatter plots, box-whisker plots, bar plot, dot plot, line charts using numeric data and categorical data, pie charts, bar Charts, Q-Q plot and curves. Controlling plot options using low-level plotting functions, adding lines, segments, points, polygon, grid to the plotting region; Add text using legend, text,

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mtex; and modify/add axes, putting multiple plots on a single page. Built in R – syntaxes for one-way ANOVA, two- way ANOVA.

# **BOOKS FOR STUDY:**

- 1) Dr. Mark Gardener (2012): *Beginning R The Statistical Programming Language*, Wiley India Pvt Ltd.
- 2) W.N. Venables and D.M. Smith (2016): An Introduction to R
- 3) J.P. Lander (2014): R for Everyone, Pearson Publications
- 4) Garrrett Grolemund: Hands-On Programming with R

# **BOOKS FOR REFERENCES:**

- 1) De Vries, A., and Meys, J. (2016). *R For Dummies*, Second Edition, John Wiley & Sons Private Ltd, NY
- 2) Crawley, M, J. (2007). The R Book, John Wiley and Sons Private Ltd., NY.

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# **SEMESTER-I**

103ST24: Estimation

#### UNIT-I:

Concepts of population, parameter (scalar, vector), parametric space, sample, sample space, statistic, estimator, estimate, sampling distribution, standard error, etc. Problem of point estimation, properties of good estimator, sufficiency- concept with examples, distinction between joint density and likelihood function. Fisher Neyman Factorization theorem. Complete sufficiency-examples, Exponential class, Minimal sufficiency.

# **UNIT-II:**

Unbiasedness-concept, examples, properties, LMVUE, UMVUE, regularity conditions, Cramer-Rao Inequality and condition(s) for existence equality, examples of construction of UMVUE using Cramer-Rao Inequality, Rao-Blackwell Theorem, Lehmann-Scheffe Theorem, Necessary and Sufficient condition for the existence of MVUE. Minimum Mean Square Error (MMSE) Estimation. Consistency-Concept and examples, necessary condition for the existence of consistent estimator, efficiency, asymptotic relative Efficiency (ARE), CAN, CAUN estimators.

# **UNIT-III:**

Moment method of Estimation, ML method of Estimation, Percentile estimation, Minimum Chi-square and Modified Minimum Chi-square.

#### UNIT-IV:

Interval Estimation, Confidence level, Construction of Confidence intervals using pivots, shortest expected length, UMA, UMAU Confidence sets. Relationship between confidence estimation and testing of hypothesis. Priori and posteriori distributions, loss function, risk function, Minmax & Bayes Estimator.

# **UNIT-V:**

Censored and truncated distributions: Type 1 and Type 2 Censoring for normal and exponential distributions and their MLE's. Interval estimation: Confidence Intervals, using pivots; shortest expected length confidence intervals.

### **BOOKS FOR STUDY:**

- 1) Statistical Inference by H.C,. Saxena & Surendran.
- 2) An Introduction to Probability and Statistics by V.K.Rohatgi and A.K.Md.E.Saleh(2001).
- Mathematical Statistics- Parimal Mukopadhyay(1996), New Central Book Agency
   (P) Ltd., Calcutta.

#### **BOOKS FOR REFERENCES:**

- 1) An Outline of Statistical Theory, Vol.II by A.M.Goom, M.K. Gupta and B. Dasgupta (1980), World Press, Calcutta.
- 2) Linear Statistical Inference and its Application by C.R. RAO (1973), John Wiley.
- 3) A First Course on Parametric Inference by B.K. kale(1999) Narosa Publishing Co.,
- 4) Lehman, E. L., and Cassella, G. (1998). Theory of Point Estimation, Second Edition, Springer, NY.

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#### **SEMESTER-I**

104ST24: Sampling Theory

# **UNIT-I:**

Systematic Sampling: Allocation problem in stratified sampling, gain in precision due to stratification, estimation of sample size with continuous data, stratified sampling for proportions, Methods of populations with linear trend: Yates end correction, Modified systematic sampling, balanced systematic sampling, centrally located sampling, circular systematic sampling.

#### **UNIT-II:**

Varying probability and Cluster sampling: Cluster sampling with equal and unequal cluster sizes, optimum cluster size for fixed cost. PPS sampling with and without replacements, procedures of selection of a sample, estimator of population total and its sampling variance in PPS with replacement, Des Raj and Murthy's estimator (for sample size two), Horvitz-Thomson estimator, Grundy's estimator, Midzuno-Sen Sampling Scheme.

#### UNIT-III:

Two-stage sampling: Two-stage sampling with equal number of second stage units, estimation of population mean, its variance and estimation of variance. Double sampling (two-phase sampling) for stratification, variance of the estimated mean, optimum allocation in double sampling.

# **UNIT-IV:**

Multiphase Sampling: Introduction, Double sampling for Difference estimation. Double sampling for ratio estimation. Double sampling for regression estimator, Optimum allocation varying probability sampling. Non sampling errors: Sources and types of non Sampling errors, Non response errors, techniques for adjustment of non response, Hansen and Hurwitz Technique, Deming's Model.

#### UNIT-V

Ratio Estimator: Introduction, Bias and Mean square error, Estimation of variance, confidence interval, comparison with mean per unit estimator, Ratio estimator in stratified random sampling. Difference estimator and Regression estimator: Introduction, Difference estimator, Difference estimator in stratified sampling. Regression estimator, Comparison of regression estimator with mean per unit estimator and ratio estimator. Regression estimator instratified sampling.

# **BOOKS FOR STUDY:**

- 1) Sampling techniques by W.G. Cochran, John Wiley
- 2) Sampling theory by Singh & Chaudhary
- 3) Sampling Theory, Narosa Publication by Des Raj and Chandok (1998)
- 4) Sampling Theory and Methods, Narosa Publishers by S. Sampath (2001)
- 5) Theory and Analysis of Sample Survey Designs, F.S. Chaudhary: New Age International Publishers, Delhi.

# **BOOKS FOR REFERENCES:**

- 1) Sampling Theory & Methods by M.N. Murthy.
- 2) Sampling theory of surveys with Applications: P.V.Sukhatme & B.V. Sukhatme.
- 3) Theory and methods of survey sampling. Mukhopadhyay(1988).

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# M.Sc. Statistics Syllabus SEMESTER- I

# 105ST24: PRACTICAL- I Statistical Software using R (Papers on 101ST24 and 102ST24) LIST OF PRACTICALS

# 101ST24 - PROBABILITY THEORY AND DISTRIBUTIONS

# Practical 1: Fitting of binomial distribution and test for goodness of fit

1. Write R-Code for fitting of binomial distribution and test for goodness of fit. Execute your R-code for the following data.

A die is thrown 60 times with the following results.

Face	1 .	2	3	4	5	6
Frequency	8	7	12	8	14	11

# Practical 2: Fitting of poisson distribution and test for goodness of fit

2. The following table gives the count of yeast cells in square of a cyclometer. A square millimeter is divided into 400 equal squares and the number of these squares containing 0,1,2,...cells are recorded.

Number of cells	0	1	2	3	4	5	6	7	8	9	10
Frequency	2	18	43	53	86	70	54	37	18	10	5
Number of cells	11	12	13	14	15	16				100	
Frequency	2	2	0	0	0	0					

Fit a poisson distribution to the data and test the goodness of fit.

# Practical 3: Fitting of normal distribution and test for goodness of fit

3. Write the necessary R code for solving the following problem and execute the same on the system. Fit normal distribution to the following data and test for goodness of fit.

Marks (X)	No. of Students
15-19	9
20-24	11
25-29	10
30-34	44
35-39	45
40-44	54
45-49	37
50-54	36
55-59	8
60-64	5
65-69	1

# Practical 4: Fitting of logistic distribution and test for goodness of fit

4. Write the necessary R code for solving the following problem and execute the same on the system. Fit a logistic distribution to the following data and test for goodness of fit.

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Page 1 of 5

Class Interval	Frequency
11-13	08
13-15	24
15-17	42
17-19	65
19-21	36
21-23	16
23-25	09

# Practical 5: Fitting of exponential distribution and test for goodness of fit

5. Write the necessary R code for solving the following problem and execute the same on the system.

The distribution of age at the marriage of grooms with brides of the following groups:

15-19	19-23	23-27	27-31	31-35
08	25	42	18	07
	15 17		10 17	13-17 17 23 10

Fit exponential distribution for the given data and also test whether the fit is good fit or not.

# Practical 6: Practical based on application of Multinomial Distribution.

- 6. A company is conducting a survey with 100 respondents, and they are asked to choose one of 3 options for a new product (let's call them Option A, Option B, and Option C). The probabilities of each option being selected are:
  - Option A: 0.4 **Option B: 0.35**
  - **Option C: 0.25**

The company wants to model the number of respondents choosing each option in 100 trials.

# Practical 7: Practical based on Conditional Probability

7. In a deck of 52 playing cards, what is the probability of drawing a heart given that the card drawn is a red card? (Recall that there are 26 red cards, and half of them are hearts).

# Practical 8: Practical based on Geometrical Probability

8. Buffon's Needle is a famous problem in probability. You drop a needle of length 1 onto a floor with parallel lines spaced d apart. The goal is to estimate the probability that the needle will cross one of the lines.

For simplicity, let the needle length l = d, which is the simplest case. The probability of crossing a line is given by the formula  $P=\pi/2$ .

We'll simulate this experiment and estimate the probability by dropping a needle many times.

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Page 2 of 5

# 102ST24 - STATISTICAL COMPUTING USING R

# Practical 1: Computing of Mean, Median, Geometric Mean and SD

**Problem:** Write a R code for computing Mean, Median, Geometric Mean and SD for the frequency distribution.

Execute R-code for the following data

Marks	15-19	20-24	25-29	30-34	35-39	40-44	45-49	50-54	55-59	60-64	65-69
No. of	9	11	10	44	45	54	37	36	18	5	1
Students											

# **Practical 2: One Sample t-Test**

**Problem:** A random sample of 10 students had the following I.Q.

70, 120, 110, 101, 88, 85, 95, 98, 107, 100.

Do this data support the assumptions of a population mean I.Q. of 100?

# **Practical 3: Two Sample t-Test**

Problem: Below are given the gain in weights (in kgs) of pigs fat of two digits A and B

Diet A	25	32	30	34	24	14	32	24	30	31	35	25	-	-	-
Diet B	44	34	22	10	47	31	40	30	32	35	18	21	35	29	22

# Practical 4: Newton – Raphson Method

**Problem:** Solve the equation  $x^3-2x-5=0$  using Newton – Raphson method by writing necessary R-code and executing the same.

# Practical 5: Completely Randomized Design (CRD)

**Problem:** The weights in gm of a number of copper wires, each of length 1 meter, were obtained. These are classified according to the die from which they come.

Die No.				
I	II	III	IV	V
1.30	1.28	1.32	1.31	1.30
1.32	1.35	1.29	1.29	1.32
1.36	1.33	1.31	1.33	1.30
1.35	1.34	1.28	1.31	1.33
1.32	NA	1.33	1.32	NA
1.37	NA	1.30	NA	NA

Setup an analysis of variance table to test the significance of the difference between the weights due to different dies. Compute CRD analysis in R.

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Page 3 of 5

# Practical 6: Randomized Block Design (RBD)

**Problem:** Setup a table of analysis of variance for yields of three strains of wheat planted in five randomized blocks.

Strains	1.367		Blocks		
A	20	21	23	16	20
В	18	20	17	15	25
C	25	28	22	28	32

Write the necessary R code for RBD analysis

# **Practical 7: Fitting Regression Lines**

Problem: A group of students recorded their study hours and corresponding exam scores:

Study Hours: 2, 3, 5, 7, 8, 10, 12, 14

Exam Scores: 50, 55, 65, 70, 75, 80, 90, 95

Analyze the relationship between study hours and exam scores by fitting a regression line.

# Practical 8: High-Level Plotting - Creating Different Types of Plots

# Problem

Consider a dataset containing the monthly sales (in thousands) of a product in different regions:

# Practical 9: Low-Level Plotting - Adding Elements to a Plot

Problem: For the following dataset:

X values: 1, 2, 3, 4, 5, 6, 7, 8

Y values: 2, 4, 6, 8, 10, 12, 14, 16

Create a scatter plot and customize it by adding:

- A horizontal reference line at Y=10.
- A vertical reference line at X=5.
- Gridlines and custom points.

# Practical 10: Q-Q Plot and Pie Chart

Problem: Given the following datasets:

- 1. Normal data:  $X = \{2,4,6,8,10,12,14,16\}$ .
- 2. Categories: A (25%), B (35%), C (20%), D (20%).

# Create:

- 1. A Q-Q plot to check normality for X.
- 2. A pie chart to visualize the categorical proportions.

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Page 4 of 5

# M.Sc. Statistics Syllabus SEMESTER - I

106ST24: PRACTICAL- II (Papers on 103ST24 and 104ST24)

# LIST OF PRACTICALS

# 103ST24 - ESTIMATION

- 1. Finding of Sufficient estimators
- 2. Finding of Unbiased estimators and consistent estimators
- 3. Finding of Efficient estimators and relative efficiency of estimators
- 4. Problems on Cramer- Rao inequality and MVB estimators and UMVUE
- 5. Estimation using Minimum chi-square method
- 6. Estimation using Modified Minimum chi-square method
- 7. Estimation using Method of Maximum likelihood
- 8. Estimation using Method of Moments
- 9. Problems on Confidence Intervals for mean and difference of means
- 10. Problems on Confidence Intervals for proportions.

# 104ST24 - SAMPLING THEORY

- 1. Stratified Sampling
- 2. Gain in Precision Due to Stratification
- 3. PPS Sampling
- 4. Gain Efficiency in Stratified Random Sampling
- 5. Precision of Systematic Sampling and Stratified Sampling
- 6. Unbiased Estimator of the Population Mean for Systematic Sampling
- 7. Yield of Average and Standard Error
- 8. Estimate the Intra-Class Correlation Co-Efficient
- 9. Ratio Method of Estimation
- 10. Regression Method of Estimation.

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# M.Sc. – Statistics Syllabus SEMESTER-II 201ST24: Multivariate Analysis

# **UNIT-I:**

The multivariate normal distribution and estimation: The multivariate normal distribution and its properties. Characteristic function of multivariate normal distribution. Sampling from multivariate normal distribution and maximum likelihood estimation, sampling distributions of Sample mean and sample covariance matrix.

# **UNIT-II:**

Inference: Wishart's distribution and it's properties. Definition of Hotelling's  $T^2$ -distribution (statistic). Invariance property of Hotelling's  $T^2$ -statistic. Application of  $T^2$  statistic in tests of mean vector(s) in case of one and two multivariate normal populations. The likelihood ratio principle. Mahalanobis  $D^2$ -statistic and it's relation with  $T^2$ -statistic. Multivariate analysis of variances (MANOVA) for one way classification.

# **UNIT-III:**

**Discriminant Analysis**: Classification and discrimination procedures for discrimination between two multivariate normal populations, Fisher's discriminant function—separation of two multivariate populations. Classification with several multivariate normal populations. Fisher's method for discrimination among several multivariate populations.

# **UNIT-IV:**

Cluster Analysis: Similarity measures, Euclidian distance and Mahalanobis squared distance-D<sup>2</sup> between two p-dimensional observations (items). Hierarchical Clustering methods - Single Linkage, Complete Linkage, Average Linkage, Ward's method and Centroid Linkage methods. Non-Hierarchical Clustering methods-K-Means method. Multidimensional scaling. UNIT-V:

**Special topics:** Principle components analysis - definition, derivation, properties and Computation. Canonical variates and canonical correlations - definition, derivation and computation. Factor Analysis - Orthogonal factor model, Methods of estimating factor loadings - the principal component method and maximum likelihood methods of estimation. Factor rotation: orthogonal factor rotation, varimax rotation.

# **BOOKS FOR STUDY:**

- Anderson, T.W.(2000). An Introduction to Multivariate Statistical Analysis, 3<sup>rd</sup> Edition, Wiley Eastern
- Johnson, A. and Wichern, D.W.(2001). Applied Multivariate Statistical Analysis, Prentice Hall and International Mardia, K.V. Multivariate Analysis

# **BOOKS FOR REFERENCES:**

- 1) Gin. N. C. (1977): Multivariate Statistical Inference. Academic Press
- 2) Seber, G. A. F. (1984): Multivariate Observations. Wiley
- 3) Kshirsagar, A. M. (1972): Multivariate Analysis, Marcel Dekker
- 4) Morrison. D. F. (1976): Multivariate Statistical Methods, 2<sup>nd</sup> Ed. McGraw Hill
- 5) Muirhead, R. J. (1982): Aspects of Multivariate Statistical Theory, J. Wiley
- 6) Rao, C. R. (1973): Linear Statistical Inference and its Applications, 2<sup>nd</sup> ed. Wiley
- 7) Sharma. S. (1996): Applied Multivariate Techniques, Wiley
- 8) Srivastava, M. S. and Khatri, C. G. (1979): An Introduction to Multivariate Statistics, North Holland.

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# M.Sc. – Statistics Syllabus SEMESTER-II

202ST24: Testing of Hypothesis

#### **UNIT-I:**

Tests of hypotheses, concept of critical region, critical function, two kinds of errors, power function, level of significance, MP and UMP tests, Neyman Pearson lemma, Randomized and Non Randomized tests.

#### **UNIT-II:**

Generalized NP-lemma, UMP tests for simple null hypothesis against one sided alternatives, and for one sided null against one sided alternative in one parameter exponential family, extension of these results to distributions with MLR property, nonexistence of UMP test for simple null against two sided alternatives in one parameter exponential family.

#### **UNIT-III:**

UMP unbiased tests and LMP tests. Similar regions, Neyman structure, Likelihood ratio test, properties of LR test, asymptotic distribution of LR test.

# **UNIT-IV:**

Chi-square and kolmogorov Smirnov tests for goodness of fit, Kendall's tau statistic, Kruskal-Wallis test, Friedman's two-way analysis of variance by ranks, Bartlett's test for homogeneity of variances, chi-square test for homogeneity of correlation coefficients, F-test for homogeneity of regression coefficients, variance stabilizing transformation and large sample tests.

# **UNIT-V:**

Notion of sequential tests, SPRT, Wald's fundamental identity, relation between the quantities A,B, alpha and beta, OC and ASN functions of SPRT, application to binomial, Poisson and normal distributions, efficiency of a sequential test.

# **BOOKS FOR STUDY:**

- 1) Statistical Inference by H.C, Saxena & Surendran
- 2) An outline of Statistical Theory vol.2 by A.M. Goon and B. Das Gupta.
- 3) An Introduction to probability and Mathematical Statistics by V.K. Rohatgi.
- 4) Mathematical Statistics- Parimal Mukopadhyay(1996), New Central Book Agency (P)Ltd., Calcutta.

# **BOOKS FOR REFERENCES:**

- 1) Advanced Theory of Statistics VOL.II by M.G. Kendall & A. Stuart.
- 2) Introduction to Mathematical Statistics by R.V. Hogg & A.T. Craig.
- 3) Linear Statistical Inference and applications by C.R. Rao.

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#### **SEMESTER-II**

# 203ST24: Theory of Linear Estimation and Analysis of Variance

#### UNIT-I:

Matrix algebra- Fundamental definitions, determinants, rank of a matrix, inverse of a matrix, orthogonal matrix, idempotent matrix, characteristic roots and vectors of a matrix. Numerical computation of characteristic roots and vectors for a positive definite matrix. Reduction of a positive definite matrix to a diagonal form using an Orthogonal matrix and non-singular matrix. Cauley-Hamilton theorem, trace of a matrix. Quadratic forms, reduction of quadratic forms using orthogonal transformation, statement of Cochran's theorem for quadratic forms.

# **UNIT-II:**

Theory of linear estimation, linear models, estimability of linear parametric function, best linear unbiased estimator, Gauss-Markov set-up, Gauss-Markov theorem, generalized linear model, generalized Gauss-Markov theorem (Atken's theorem).

#### **UNIT-III:**

Decomposition of sum of squares in analysis of variance one way classification, two way classification with equal and unequal number of observations per cell. Multiple comparisons; Fisher's least significance difference test and Duncan's multiple range test, Fixed, random and mixed effect models.

# **UNIT-IV:**

Analysis of covariance of one way and two way classification, applications to standard designs-CRD,RBD missing plot technique- general theory and applications to RBD and LSD.

# **UNIT-V:**

Model Adequacy checking: Test for Normality, Test for equality of Variances (Bartlett test, Modified Levene Method). Multiple comparison tests: Turkey's test, The Fisher Least significant Difference (LSD) method, Duncan's Multiple range test.

# **BOOKS FOR STUDY:**

- 1) Montgomery, D.C, (1976), Design and Analysis of experiments., John Wiley & sons.
- 2) Joshi, D.D.(1987), Linear Estimation and Design of experiments., Wiley Eastern Ltd.
- 3) Das, M.N. and Giri, N.C. (1986), Design and An Analysis of Experiments, Wiley Eastern Ltd.

# **BOOKS FOR REFERENCES:**

- 1) Datta, K.B. (2000)., Matrix and Linear Algebra
- 2) Rangaswamy, R, (1995), A text book of Agricultural Statistics., New Age international Publishers Limited.
- 3) Kempthorne, O, (1951)., The design and Analysis of Experiments., Wiley Eastern Private Limited.
- 4) Rao, C.R, (1983)., Linear Statistical inference and its applications., Wiley Eastern Ltd.
- 5) Raghavarao, D.(1987), statistical Techniques in Agricultural and Biological Research., Oxford & IBH publishing Company Private limited.
- 6) Federer, W.t (1967), Experimental Design Theory and Application, Oxford & IBH publishing company.
- 7) Biswas, S. (1984). Topics in Algebra of Matrices, Academic Publication.

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# M.Sc. – Statistics Syllabus SEMESTER-II

# 204ST24: Linear Models and Applied Regression Analysis

#### **UNIT-I**

Gauss-Markov set-up, Normal equations and Least squares estimates, variances and covariances of least squares estimates, estimation of error variance.

#### **UNIT-II**

Estimation with correlated observations, least squares estimates with restriction on parameters, simultaneous estimates of linear parametric functions.

### **UNIT-III**

Tests of hypotheses for one and more than one linear parametric functions, confidence intervals and regions. Analysis of Variance.

#### **UNIT-IV**

Simple linear regression, multiple regression, fit of polynomials and use of orthogonal polynomials.

# **UNIT-V**

Multicollinearity, Ridge regression and principal component regression, subset selection of explanatory variables.

# **BOOKS FOR STUDY:**

- 1) Graybill, F.A. (1983): Matrices with Applications in Statistics. Wadsworth.
- Draper, N.R. and Smith, H (1998): Applied Regression Analysis. 3<sup>rd</sup>Edition. Wiley-Blackwell.
- 3) Douglas C. Montgomery, Elizabeth A. Peck and G. Geoffrey Vining (2012): Introduction to Linear Regression Analysis 5<sup>th</sup> Edition. Wiley
- 4) Goon, Gupta and Das Gupta (2003): An outline of Statistical Theory. Volume II. The World Press Pvt. Ltd.

# **BOOKS FOR REFERENCES:**

- 1) Bapat.R.B. (2012): Linear Algebra and Linear Models. 3<sup>rd</sup> Edition. Springer.
- 2) Cook, R.D. and Weisberg, S. (1983): Residual and Influence in Regression. 1st Edition. Chapman and Hall.
- 3) Johnson, J. (1996): Econometric Methods, 4th Edition. McGraw Hill.
- 4) Rao, C.R. (2002): Linear Statistical Inference and Its Applications. 2<sup>nd</sup> Edition. Wiley-Blackwell.
- 5) Weisberg, S. (2013): Applied Linear Regression. 4th Edition. Wiley.

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# M.Sc. – Statistics Syllabus SEMESTER-III

# 301ST24: Design of Experiments

#### UNIT-I:

General factorial experiments, factorial effects, best estimates and testing the significance of factorial effects, estimation of main effects, interaction and analysis of 2<sup>n</sup> factorial experiments in general with particular reference to n=2,3. 3<sup>2</sup> and 3<sup>3</sup> factorial experiments. Total and partial confounding in case of 2<sup>n</sup> (for n=2.3), 3<sup>2</sup> and 3<sup>3</sup> factorial designs.

# **UNIT-II**

Incomplete block designs; balanced Incomplete block designs (BIBD), parametric relations, intra block analysis, simple methods of constructions of BIBD, resolvable and affine resolvable designs, Partially Balanced Incomplete Block Designs (PBIBD) with two associateclasses, parametric relations, intra block analysis.

#### **UNIT-III:**

Youden square design, simple lattice design, split plot design, strip plot design and their analysis, Gracco latin square design.

#### **UNIT-IV:**

Concept of response surface methodology (RSM), response surface designs, linear response surface designs, second order response surface designs, variance of estimated second order response surface, Rotatable designs; conditions for second order rotatable designs, construction of second order rotatable designs using central composite designs, Balanced incomplete block designs.

# UNIT-V:

Taguchi Method, Taguchi Philosophy, Loss Functions, Signal-to-Noise Ratio and Performance Measures, Critique of S/N Ratios. Experimental Design in the Taguchi Method. Parameter Design in the Taguchi Method.

# **BOOKS FOR STUDY:**

- 1) M.N. Das and N.C. Giri. (1986), Designs and Analysis of Experiments, Wiley Eastern Ltd.
- 2) Montgomery, D.C, (1976)., Design and Analysis of Experiments, John Wiley & sons.
- 3) D.D.Joshi. (1987), Linear Estimation and Design of Experiments, Wiley Eastern Ltd.
- 4) Taguchi Engineering by Philippe ross.

# **BOOKS FOR REFERENCES:**

- 1) Raghavarao, D. (1971), Constructions and Combinatorial Problems in Design of Experiments, John Wiley & Sons, Inc.
- 2) W.G. Cochran and G.M. Cox, (1957), Experimental designs, A wiley International Edition.
- 3) Box, G.E.P. and Draper, N.R. (1986), Empirical Model-Building and Response surfaces, John Wiley & Sons.
- 4) R.H. Myers. (1976), Response Surface Methodology, Allyn and Bacon, Boston
- 5) Aloke Dey. (1986), Theory of Block Designs, Wiley Eastern Limited.
- 6) Oscar Kempthorne (1951), The Design and Analysis of Experiments., Wiley Eastern Private Limited.
- 7) Walter T.Federer (1967)., Experimental Design Theory and Application., Oxford & IBH Publishing Company.

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# M.Sc. – Statistics Syllabus SEMESTER-III

# **302ST24: Statistical Quality Control**

# UNIT - I:

The X and S control charts with variable sample size. The  $S^2$  control chart. The Shewart Control Chart for individual measurements. Control charts for multiple stream process and group control charts. Economic design of control charts: designing a control chart, process characteristics, cost parameters, early work & semi-economic designs and an economic model of the X control chart.

# UNIT - II:

The Cumulative Sum (CUSUM) control chart - Basic principles, the tabular or algorithmic CUSUM for monitoring the process mean, recommendations for CUSUM design. The standardized CUSUM, rational subgroups, one sided CUSUMs, CUSUM for monitoring process variability, CUSUMs for other sample statistics. The V-Mask procedure. The exponentially weighted moving average (EWMA) control chart - Design of a EWMA control chart, rational sub group, robustness of the EWMA to non-normality, extension of the EWMA. The moving average control chart.

# UNIT - III:

Statistical process control for short production runs - X and R charts for short production runs, attribute control charts for short production runs. Modified and acceptance control charts - modified control limits for X chart, acceptance control charts, control chart for a "Six-Sigma" process.

# UNIT-IV:

The multivariate process monitoring and control: description of multivariate data, the multivariate normal distribution, the sample mean vector and covariance matrix. The Hotelling  $T^2$  control chart. The multivariate exponential weighted moving average (EWMA) control chart. Control chart for monitoring variability. Latest structure methods: principal component and partial least squares.

# UNIT-V:

Tools and Techniques of Total Quality Management (TQM), techniques for analyzing a quality process, SPC as a tool of quality management, Quality systems – ISO 9000 standards, QS-9000 standards, Bench marking practices and Quality Auditing Notion of Six – sigma and its uses.

# **BOOKS FOR STUDY:**

- 1) R.C. Guptha(2001): Statistical Quality Control. 9th Edition. Khanna Publishers.
- 2) Duncan Acheson (1986): Quality Control and Industrial Statistics. 5th Edition. Irvin.
- 3) Statistical Quality Control 7<sup>th</sup> edition, E.L. Grant & R.S. Leavenworth; McGraw Hill, New York.

# **BOOKS FOR REFERENCES:**

- 1) Cowden D J (1957): Statistical Methods in Quality Control. 1st Edition. Prentice-Hall Inc.
- 2) Mittag and Rinne (1993): Statistical Methods for Quality Assurance. 2<sup>nd</sup> Edition. Chapman and Hall Ltd.
- 3) Montgomerv. D.C (2012): Introduction to Statistical Quality Control. 7<sup>th</sup> Edition. John Wiley and Sons

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# M.Sc. – Statistics Syllabus SEMESTER-III 303ST24: Actuarial Statistics

#### UNIT-I:

Effective Rate of interest - Nominal rate of interest - Force of interest Effective rate of interest corresponding to Nominal rate of interest and Force of interest - Accumulation of 1 unit corresponding to the given rate of interest present value of 1 unit due at the end of n years corresponding to the given rate of interest, effective rate of discount-Nominal rate of discount - Force of interest varying continuously.

#### **UNIT-II:**

Definition of Annuity - Present value and Accumulation of an Immediate annuity - Annuity due - Present value and Accumulation of an Annuity - due - Present value and Accumulation of a Perpetuity and Perpetuity - due-Increasing and Decreasing Annuities. Annuities where payments are made continuously.

#### **UNIT-III:**

Analysis of Annuity payments - Loan installment - Principal and interest portions of a typical loan installment - General Expression for principal and interest portion - Purchase price of an annuity net of tax. Independent annual interest rates - Mean and Variance of the accumulation of a single investment, viz  $E(S_n)$  and  $V(S_n)$  - Mean and Variance of the accumulation of a series of investments, viz  $E(A_n)$  and  $V(A_n)$  - Mean and Variance of a present value of unit due at the end of n years, viz  $E(V_n)$  and  $V(V_n)$ . Dependent annual interest rates and simple problems.

#### **UNIT-IV:**

Net present value (NPV) - Internal rate of return (IRR)- Interpretation of NPV and IRR- Comparison of two investment projects - Discounted Payback Period - The effect of inflation on IRR- Money weighted rate of return (MWRR) - Time weighted rate of return (WRR) - linked internal rate of return(LIRR).

# **UNIT-V:**

Multiple life functions, joint life and last survivor status, insurance and annuity benefits through multiple life functions, evaluation for special mortality laws. Multiple decrement models, deterministic and random survivorship groups, associated single decrement tables, central rates of multiple decrements, central force assumptions for multiple decrements. Uniform distribution assumption for multiple decrements.

# **BOOKS FOR STUDY:**

- 1) Fundamentals of Actuarial Mathematics, Promislow, S.D(2006): John Willey, Chapters 2-11 &14.
- Newton L. Bowers, Jr, Hans U. Gerber, James C. Hickmann, Donald A. Jones and Cecil J. Nesbitt (1997): Actuarial Mathematics, The Society of Actuaries.
- 3) Compound Interest and Annuities certain by D.W.A. Donald, Heinemann, London.
- 4) An Introduction to Mathematics of Finance, Butter Worth & Heinemann by J. J. McCutcheon and W.F.Scott.
- 5) Gnana Deep Study Maeraials.

# **BOOKS FOR REFERENCES:**

- 1) Actuarial mathematics by N.L. Bowers, H.U. Gerber, J.C. Hickman, D.A. Jones and C.J. Nesbitt Published by society of Actuaries, Ithaca, Illinois, U.S.A. Second Edition (1997) Chapters: 1,2,3,4,5,9 &10
- 2) Life Contingencies, by Spurgeon Cambridge University Press.
- 3) Life Contingencies, Heinemann. Neill, A. (1977).
- 4) An Introduction to Actuarial Studies, Atkinson and Dickson (2011): Edward Publishing.
- 5) Life Contigencies by A. Neile Published by Heineman.
- 6) Modern Actuarial Theory and Practice, Philip, M. et. al (2004): Chapman and Hall.

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# M.Sc. – Statistics Syllabus SEMESTER-III 304ST24: Reliability-I

#### **UNIT-I**

Importance of reliability, definition of reliability and its measures, concept of failure. General provision of a reliability specification, Methods of achieving reliability, Broad functions of reliability. Bath tub curve, causes of early failure and methods to avoid them.

#### **UNIT-II**

Life distributions; reliability function, hazard rate, Common failure distributions: exponential, weibull, truncated normal, log normal - their properties and uses and Estimation of parameters and tests in these models.

# **UNIT-III**

Series, parallel and r-out of n configurations; their block diagram, reliability graph and determination of reliability through combinatorial methods. Events space, cut set and tie set, Multistate models.

#### **UNIT-IV**

System reliability with exponential components in series, parallel and r- out of - n system. Usefulness of redundancy and improvement factor. MTTF, MTBF, Equivalents MTBF of series and parallel system. Cold and hot redundancy, reliability of stand-by system. Weakest link model, chain model, stress-strength model, non-parametric estimation of reliability.

# **UNIT-V**

Problem of life testing, estimation of parameters and reliability in standard probability models (Exponential, Weibull, Normal) using complete samples. Probability plotting and graphical procedures for estimating the parameter and testing validity of model by some standard statistical tests.

# **BOOKS FOR STUDY:**

- 1) Probability Distributions Used in Reliability Engineering, Andrew N.O'Connor Mohammad Modarres, Ali Mosleh; Published by the Center for Risk and Reliability
- 2) Statistical Analysis of Reliability and Life-Testing Models, Bain, L.J. Dekker, New York
- 3) Statistical Models and Methods for Lifetime Data, Lawless, J.F., Wiley, New York
- 4) Bayesian Reliability Analysis, Martz, H.E. & Weller, A., Willey New York
- 5) Statistical Theory of Reliability and Life Testing Probability Models, Barlow R.E.& Proschan, F., Holt, Rinehart and Winston, New York
- 6) Reliability and Life Testing, Sinha, S.K., Wiley Eastern Limited

# **BOOKS FOR REFERENCES:**

- 1) Applied Life Data Analysis, Nelson, W. (1982):, John Willey
- 2) Software Engineering: Design, Reliability and Management, Shooman, M.L., McGraw-Hill, New York
- Reliability in Engineering Design, Kapur, K.C. and Lamberson, L.R., John Wiley, N.York
- 4) J.V. Deshpande and Sudha G. Purohit (2005) Life time data: Statistical Models and Methods World Scientific
- 5) Introduction to Reliability Analysis, Zacks S (1992), Springer Verlag, New York
- 6) Applied Reliability 3rd Edition by Paul A. Tobias, CRC Press Taylor & Francis Group.

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# M.Sc. - Statistics Syllabus **SEMESTER-IV 401ST24: Econometrics**

# **UNIT-I**

Simple Regression Analysis: What is Econometrics? Methodology of Econometrics. Simple linear model and assumptions, Least-Squares Estimators and their properties. ML estimation of the parameters. Statistical Inference and prediction with the simple regression model. Regression analysis versus Correlation analysis, Regression analysis and ANOVA. Other functional forms of regression models -Log-linear, Semilog, reciprocal and logarithmic reciprocal models.

#### **UNIT-II**

Multiple Regression Analysis: The general linear model (GLM) and assumptions of the model, ordinary least squares (OLS) and ML estimation, properties of OLS estimators (Gauss-Markov theorem). The coefficient of determination  $R^2$ , and Adjusted  $R^2$  or  $\overline{R^2}$ .

Inferences about regression model, problems of prediction. Linear restrictions-- restricted least squares.

# **UNIT-III**

Testing the structural change in regression models, Chow test for testing the equality of two regression equations. The use of dummy variables in multiple regression. The problem of multicollenearity - nature, sources, consequences, diagnostics (variance inflation factors and condition index) and remedies (Ridge regression and principle component regression methods). Aitken's generalized least squares(GLS) method.

# **UNIT-IV**

The problem of heteroscadesticity— nature, sources, consequences, detection (Glejser Test, Goldfeld-Quandt test, Breusch-Godfrey Test, Breusch-Pagan-Godfrey Test, White's test) and remedies. The problem of auto correlation-nature, sources, consequences, detection (Durbin-Watson d-test and Breusch-Godfrey (LM) Test,) and remedies (Cochrane-Orcutt iterative procedure, C-O two-step and D-W two-step methods).

#### **UNIT-V**

Special Topics: Non-Linear Regression Models, Polynomial regression models, Qualitative Response Regression Models-The LOGIT (Logistic regression) and the PROBIT models. Errors in Variables, Instrumental Variables, Autoregressive and Distributed Lag models-Koyak, Stock adjustment and partial adjustment models.

# **BOOKS FOR STUDY:**

- 1) Gujarathi, D.N., Porter, D.C. and Gunasekar, S. (2011): Basic Econometrics, 5th Edition, McGraw Hill
- 2) Johnston, J. and DiNardo, J.(1997). *Econometric Methods*, 4<sup>th</sup> Ed., McGraw Hill
- 3) Montgomery, D.C., Peck, E.A. and Geoffrey Vininig, G. (2003). Introduction to Linear Regression Analysis, 3rd Ed., Wiley
- 4) Koutsoyiannis, A (1979): Theory of Econometrics, Macmillan Press
- 5) Theil. H (1982): Introduction to the Theory and Practice of Econometrics, John Wiley. **BOOKS FOR REFERENCES:**
- 1) Apte P.G. (1990): Textbook of Econometrics. Tate McGraw Hill
- 2) Intrilligator, M.D. (1980): Econometric models Techniques and Applications, Prentice Hall of India.
- 3) Klein, L.R.(1962): An introduction to Econometrics, Prentice Hall of India
- 4) Mai Invaud, E (1966): Statistical Methods of Econometrics, North Holland.

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# M.Sc. – Statistics Syllabus SEMESTER-IV 402ST24: Acceptance Sampling Plans

# UNIT - I:

Attribute Sampling Plans: Introduction, advantages and disadvantages of sampling, Producer's risk and Consumer's risk, Operating Characteristic curve, evaluating sampling plans using average out going quality limit, average sample number. Lot-by-Lot attribute sampling plans: Single sampling plans – The OC curve, design of single sampling plans, double sampling plans, The OC curve , ASN curve, design of double sampling plan sequential sampling plan, standard sampling plans-Military Standard 105E and Dodge – Roming sampling plan.

# UNIT - II:

Acceptance sampling plans for variables, Introduction, advantages and disadvantages of sampling, variable sampling plans for a process parameter – Estimating process average – Single specification limit and known process standard deviation, estimating process average –double specification limits and known process standard deviation, estimating process average

Single specification limit and unknown process standard deviation. Standardized plans –
 MIL-STD-414, Sequential sampling plan by variables.

# UNIT - III:

Acceptance sampling procedures – importance, procedures, advantages and disadvantages of Chain sampling plan, Skip-lot sampling plan, Continuous sampling – CSP-1, CSP-2, CSP-3 and multi-level plans, Military standard sampling plan –MIL STD 1235b.

# UNIT-IV:

Industrial Experimentation, Fractional factorial experiments, Response surface methodology, Six sigma in process improvement and product development. Wald-Wolfwitz type and their properties.

#### UNIT - V:

Rectifying inspection by Lot-By-Lot Sampling: Rectifying Inspection Plans Calling for 100 Percent inspection of Rejected Lots. Rectifying Inspection Plans with less than 100 Percent inspection of Rejected Lots.

# **BOOKS FOR STUDY:**

- 1) Introduction to Statistical Quality Control, Montgomery, D.C., John Wiley (Asia) 2001.
- 2) Modern Methods for Quality Improvement, H.M.Wadsworth, K.S.StephensA.B.Godftrey, Second Edition; 2004, John Wiley and sons.
- 3) The Essence of TQM, John Bank, Printice,- Hall of India Pvt Ltd (1998).
- 4) Statistics of Quality Control Sampling Inspection and Reliability by S.Biswas, Newcentral book agency Pvt Ltd (2003).

# **BOOKS FOR REFERENCES:**

- 1) R.C. Guptha (2001): Statistical Quality Control. 9th Edition. Khanna Publishers.
- 2) Duncan Acheson (1986): Quality Control and Industrial Statistics. 5th Edition. Irvin.
- 3) Statistical Quality Control 7<sup>th</sup> edition, E.L. Grant & R.S. Leavenworth; McGraw Hill, New York.

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# M.Sc. – Statistics Syllabus SEMESTER-IV 403ST24: Operations Research

# **UNIT-I:**

Games as decision problems, Two-person Zero-Sum game, Pure and mixed Strategies, maximum criterion, dominance, minimax theorem. Solutions of 2X2, 2Xm, nX2 games and 3X3 games (using simplex algorithm).

#### **UNIT-II:**

Inventory control, models of inventory-purchase model with instantaneous replenishment and without shortages, Manufacturing model without shortages, Purchase model with instantaneous Replenishment and with shortages. Manufacturing model with shortages, Operation of inventory system, Quantity Discount - Price breaks - Purchase Inventory Model with one price break, two price breaks and any number of price breaks.

#### UNIT-III:

Queueing models - Characteristics of Queueing Systems, Classification of Queues. Steady-state solution of M/M/1/ $\infty$ /FCFS, M/M/1/N/FCFS, M/E<sub>k</sub>/1 models and M/G/1 queue - length Pollazek - Khinchine result.

# **UNIT-IV:**

Replacement and maintenance analysis-Types of maintenance, Types of replacement problems, Determination of economic life of an asset, Basics of interest formulae – Present- worth factor (P/F, i, n), Equal payment series capital recovery factor (A/P, i, n). Simple probabilistic model for items which completely fail.

# **UNIT-V:**

Project management; CPM and PERT; probability of project completion, crashing.

#### **BOOKS FOR STUDY:**

- 1) Hillier, F.S. and Leiberman(2017)G.J., Holden Dev, Introduction to Operations Research.
- 2) Sharma, J.K., 2003, Operations Research Theory and Applications, Macmillan, India
- 3) Kantiswarup, Gupta, P.G. and Man Mohan, Operations Research, Sultan Chand & Sons
- 4) S.D. Sharma, Operations Research, Kedar Nath Ram Nath & Co, Meerut
- 5) Panneerselvam. R, Operations Research, Printice Hall of India, Pvt Ltd.
- 6) Churchman, C.W., Ackoff, R.L. and Amoff, E.L. (1957). Introduction to OperationsResearch.

# **BOOKS FOR REFERENCES:**

- 1) Philps D.T. Ravindran A and Sal berg J., Operations Research, Principles and practice, John Wiley
- 2) Donald Gross and Carl M. Harrsis, Fundamentals of Queueing Theory, John Wiely
- 3) Leonard Kleinrock, Queueing System, volume 1. Wiley Inter science
- 4) Taha, HA. (1982). Operational Research
- 5) Philips, D.T., Ravindran, A. and Solberg, J. Operations Research, Principles and Practice

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# M.Sc. – Statistics Syllabus SEMESTER-IV 404ST24: Reliability-II

#### UNIT-I:

# (i) Non-Repairable System:

Single element-non repairable, two element-non-repairable system; solution through Laplacetransform. Poisson process, Stand-by system.

# (ii) Repairable System:

Reliability and availability function of one and two components system, up-time and down-time ratio, steady state probabilities.

#### **UNIT-II:**

Coherent System and its Structural Properties: Systems with independent components, coherent system, path sets and cut sets, reliability of coherent system, bounds on system reliability, Relative importance of components, Modular decomposition of coherent system and improved bounds for system reliability. Concept of associated random variables.

#### **UNIT-III:**

**Fault Tree Analysis:** Event tree, simple fault tree and its construction, Mathematics of FTA, Efficiency of FTA formats, FTA, Event space method, Monte-Carlo technique, Min-cut set algorithm, FMEA, Carrying out FMEA with practical example.

# **UNIT-IV:**

**Life distributions** – reliability function; hazard rate; common life distributions-Exponential, Gamma, Weibull, Lognormal, Pareto. Estimation of parameters and tests in these models.Life tables, mean residual life and their elementary properties.

#### **UNIT-V:**

**Notions of Ageing classes** – IFR, IFRA, NBU, DMRL and NBUE and their duals. Estimation of survival function-Acturial Estimator, Kaplan–Meier Estimator, Semi–parametric regression for failure rate–Cox's proportional hazards model with one and several covariates.

#### **BOOKS FOR STUDY:**

- 1) Reliability Engineering Theory and Practice, A. Birolini, Fourth Edition, Springer Int.
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- 4) Probability Distributions Used in Reliability Engineering, Andrew N.O'Connor Mohammad Modarres, Ali Mosleh; Published by the Center for Risk and Reliability
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